

# Formal Learning Theory

## Homework 2

(due on Friday, February 22nd at 1pm)

February 15th, 2013

**Ex. 1** Take  $E$  to be the set of all even natural numbers. Let  $\mathcal{L} = \{E \cup D_n \mid D_n \subseteq \mathbb{N}, D_n \text{ is finite}\}$ . Show that  $\mathcal{L}$  is identifiable.

**Ex. 2**

(a) Given the class of all co-singletons  $\mathcal{L}$ , and learner  $M$  discussed in class 1 and 2, that identifies the class, provide:

1. locking sequence for  $M$  and  $\mathbb{N} - \{i\}$ , and
2. tell-tale subset for  $\mathbb{N} - \{i\}$ .

(b) Modify  $M$ , to obtain  $M'$ , such that  $M'$  answers  $\mathbb{N} - \{9\}$  as long as 9 hasn't appeared, and otherwise proceeds as  $M$ , provide:

1. locking sequence for  $M$  and  $\mathbb{N} - \{i\}$ , and
2. tell-tale subset for  $\mathbb{N} - \{i\}$ .

**Ex. 3** [\*] Show that the class of all co-singletons  $\mathcal{L}$  cannot be identified incrementally. Hint: Consider a locking sequence for  $\mathbb{N} - \{0\}$ . A further hint is available on request.

**Ex. 4** Give a full proof of the following theorem discussed in class: *Any  $\mathcal{L}$  is identifiable on informant, i.e. text that give complete negative as well as positive information.*