

# Structures of Social Proof

Vincent F. Hendricks  
Rasmus K. Rendsvig

Department of Philosophy, University of Copenhagen  
vincent@hum.ku.dk -- rendsvig@gmail.com

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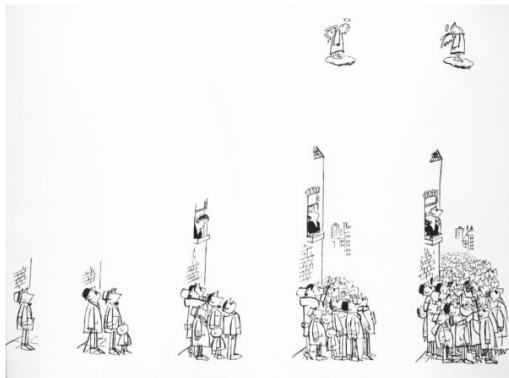
*“The task is to identify the conditions and procedures under which groups can find the information that their members have.”*

– Cass Sunstein



Forthcoming in *Socio-Epistemic Phenomena: 5 Questions*  
Edited by Vincent F. Hendricks & Rasmus K. Rendsvig  
Automatic Press / VIP, 2013

# Structures of Social Proof



**SOCIAL PROOF:** Single agents assume beliefs / norms / actions of other agents in an attempt to reflect the correct view / stance / behavior for a given situation

# Two Prominent Examples of Social Proof

# Informational Cascades



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- ▶ Examples: Bubbles in stock and real estate markets (Hendricks & Lundorff-Rasmussen, 2013)

# Bystander Effects



- ▶ BEs occur when individuals do not offer any means of help in an emergency situation to the victim when other individuals are present (social proof).



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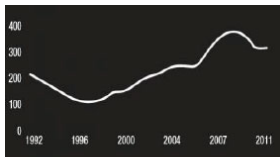
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- ▶ The greater the number of bystanders, the less likely it is that any one of them will help.
- ▶ Examples: Smokey room (Darley & Latane 1968), corporate boards (Westphal & Bednar, 2005), intervention and regulation in financial market (Hendricks & Lunderoff Rasmussen 2012).

# Bystander Effects for Real (Estate)



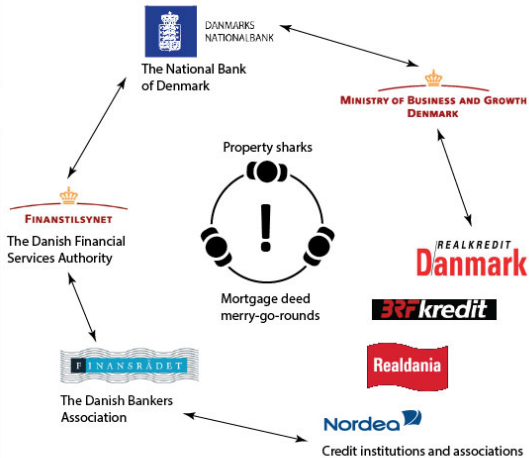
Price development on Danish corporate realty 1992-2011

## REGULATORY INTERVENTION?

*NEDTUR!*  
*Finanskrisen forstået filosofisk*

Vincent F. Hendricks & Jan Lundorff Rasmussen  
København: Gyldendal, 2012

*DOWNFALL!*  
*Philosophy and the Financial Crisis*  
Forthcoming, 2013



# Socio-Epistemic Phenomena

Subsequently socio-epistemic phenomena like:

Bandwagon effects

Boom thinking

Group thinking

Herd behavior

Gullibility

Conformity

Compliance

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also rely on social proof one way or the other

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## **The Diamond Conferences**

Amsterdam / Copenhagen / Munich / Lund, 2014-16

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- ▶ Investors may start looking for social proof to facilitate a qualified decision.

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It also means that the collective behavior of investors become susceptible to the workings of socio-epistemic phenomena like informational cascades, pluralistic ignorance, bystander effects . . .

# Socio-Epistemic Phenomena are Composites

- ▶ Agents
- ▶ Beliefs
- ▶ Private / public signals
- ▶ Preferences
- ▶ Expectations
- ▶ Modes of behavior
- ▶ ...

# The Structure of Social Proof

## Structural Ingredients

- ▶ Epistemic Logic
- ▶ Game Theory
- ▶ Judgment Aggregation
- ▶ ...

## Parameters

- ▶ Uncertainty and Information
- ▶ Decision Rules and Actions
- ▶ Interpretation Rules and Social Proof
- ▶ Belief Merge Operations
- ▶ Social Network Structure
- ▶ ...

## Modularity

- ▶ *Change module, plug module, press play*

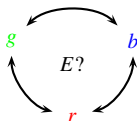


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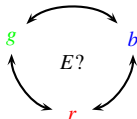
- ▶ Formalization of pluralistic ignorance explanation put forth by social psychologists.
- ▶ Epistemic Plausibility Models and Action Models + some.

# Bystander Effects in DEL



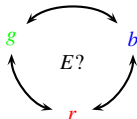
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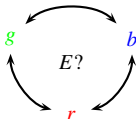
- ▶ A set of agents, that act concurrently in a number of rounds
- ▶ A situation on which the agents react
  - ▶ E.g.: Does the elderly woman need help? Is the Emperor naked? Is the CEO's suggestion correct? Is there a problem with the mortgage deed merry-go-rounds?

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- ▶ Each may choose to Help, Not Help, or Observe
  - ▶ Decisions are based on information from two sources:
    - ▶ Information from the world
    - ▶ Information extracted from the actions of others

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- ▶ Root of the Problem: Agents choose to observe in the first round, but misinterpret the same action by others.

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## Modularity and Bystander Effects: Decision

To incorporate a notion of **choice** in DEL models, we use **decision rules**. E.g.:

$$\text{First Responder: } B_i E \rightarrow [X] H_i \wedge B_i \bar{E} \rightarrow [X] \bar{H}_i^1$$

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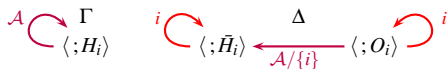
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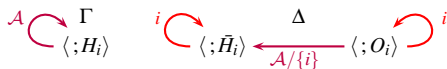
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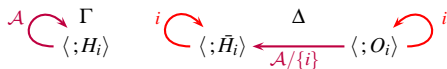
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The performed actions are not linked to beliefs; there is no assumption of rationality driving such reasoning.

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The agents now have “refined” beliefs, upon which their decisions can be based:

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- ▶ Rigorous reconstruction of the informal elements from IC models from behavioral economics.
- ▶ Epistemic Plausibility Models and Action Models + some.

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  5. Executes action

# Four Combinations

Decision Rules:

<b>1. Individualist:</b>	$(B_i L \rightarrow [X] L_i) \wedge (B_i R \rightarrow [X] R_i)$
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	Cascade?	When?	Breaks?
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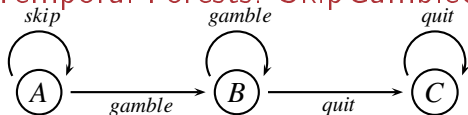
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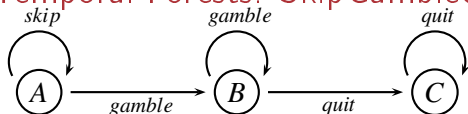
- ▶ How social proof may be extracted from the actions of others, how it may be used to influence expectations and actions in extensive games.
- ▶ Game Theory coupled with Doxastic-Epistemic Temporal Logic with Expectations + change.

## From DEL to Temporal Forests: SkipGambleQuit



**Pay-offs:** +0 for any *skip*, +1 for any *gamble* before *crash*, -1 for any *gamble* after *crash*, +0 for any *quit*.

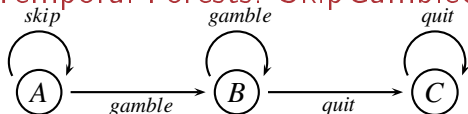
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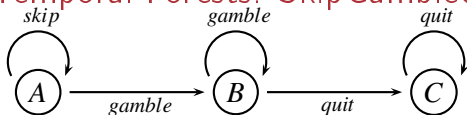


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**Adoption:** If a social-conservative agent  $i$  receives social proof from group  $G$  of which she believes that each agent is conservative, then if the majority of  $G$  played the same move in the previous round,  $i$  will play this move in the next round.



## SkipGambleQuit: Example 1

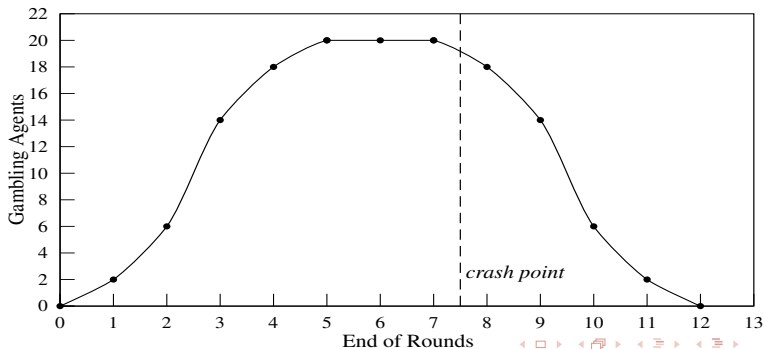
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**Example 1:** If a set of social-conservative agents end up in a state where they *Gamble* and seek information from each other, *then they will play Gamble till the end of the game.*

## SkipGambleQuit: Example 2

**Adoption:** If a social-conservative agent  $i$  receives social proof from group  $G$  of which she believes that each agent is conservative, then if the majority of  $G$  played the same move in the previous round,  $i$  will play this move in the next round.

**Example 2:** If groups of social-conservative agents herd each other in following some set of well-informed aggressive agents, a *delayed informational cascade* may occur, which results in *negative payoffs* for agents with too “old” information.



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## The New Game in Town